

LESSON
3-7

Review for Mastery
Solving Absolute-Value Inequalities

To solve an absolute-value inequality, first isolate the absolute-value expression. Then write and solve the two cases.

Solve $|x - 2| + 8 < 10$.

Step 1: Isolate the absolute-value expression.

$$|x - 2| + 8 < 10$$

$$\underline{\quad -8} \quad \underline{-8} \qquad \text{Subtract 8 from both sides.}$$

$$|x - 2| < 2$$

Step 2: Solve the two cases.

$$|x - 2| < 2 \text{ means } x - 2 > -2 \text{ AND } x - 2 < 2.$$

$$\begin{array}{ccc} \underline{+2} & \underline{+2} & \underline{+2} \quad \underline{+2} \\ x & > -2 & \text{ AND } x < 4 \end{array} \qquad \text{Solve each inequality.}$$

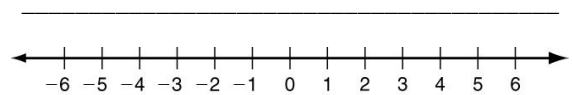
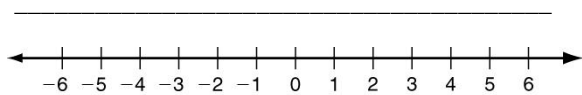
Graph the solution as shown.



Solve each inequality and graph the solutions.

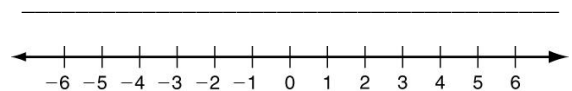
1. $|x| + 12 < 16$

2. $|x - 1| + 5 \leq 9$



3. $7|x| \leq 21$

4. $|x + 4| - 3 < -2$



LESSON
3-7

Review for Mastery

Solving Absolute-Value Inequalities (continued)

You can use a similar method to solve absolute-value inequalities that involve a greater-than symbol ($>$). As always, the first step is to isolate the absolute-value expression. Then work with the two cases.

Solve $|x - 5| - 4 > -1$.

Step 1: Isolate the absolute-value expression.

$$|x - 5| - 4 > -1$$

$$\underline{\quad\quad} + 4 \quad + 4 \qquad \text{Add 4 to both sides.}$$

$$|x - 5| > 3$$

Step 2: Solve a compound inequality.

$$|x - 5| > 3 \text{ means } x - 5 < -3 \text{ OR } x - 5 > 3.$$

$$\quad \quad \quad + 5 \quad + 5 \quad \quad + 5 \quad + 5 \quad \text{Solve each inequality.}$$

$$x < 2 \text{ OR } x > 8$$

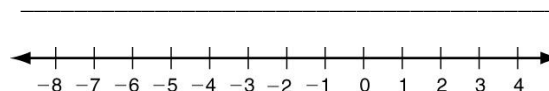
Graph the solution as shown.



Solve each inequality and graph the solutions.

5. $4 + |x| \geq 5$

6. $2|x + 2| > 6$



7. $|x| - 7 > -3$

8. $|x - 4| + 5 \geq 8$

